Intelligent Patterning

or

Why I've been doing computer science

Brief overview of where I'm headed:

- General problem solving
- Pattern recognition
- Symbols and signs
- Intelligent patterning
- Some history
- What's wrong in computing today
- The intelligent mathematical assistant

General problem solving

- Understanding the problem
 - 1. Problem context and statement of the problem
 - 2. Solving the right problem (ill-posed and ill-conditioned problems)
 - 3. Preconceptions
 - 4. Language and restating the problem
- The role of experience
 - 1. Similar problems and analogy
 - 2. Appropriate tools
 - 3. Specific experience

- Three basic methods
 - 1. Plug and grind
 - 2. Guess and prove
 - 3. Look it up
- Hypothesis generation and testing
 - 1. Flexibility and freedom willingness to try and fail
 - 2. Recognizing blind alleys, and the value of exploring
 - 3. Appropriate hypotheses
 - 4. Lateral thinking

- Recognizing solutions
 - 1. "A" solution vs. "the" solution
 - 2. Useful solutions
 - 3. When a "solution" solves an un-posed, but more significant problem

Pattern recognition

- Images ("visual patterns") vs.
 "syntactic" patterns
- Symbols as patterns, and symbols as pattern labels
- Patterns of symbols
- Hierarchies of patterns, and symbols as tools for recognizing patterns
- Pattern manipulation
- Learning to recognize patterns, and pattern recognition as learning

Pattern recognition examples

- What number comes next in the sequence?
 1, 1, 2, 3, 5, 8, 13, ...
- What number comes next in the sequence?
 8, 5, 4, 9, 1, 7, 6, 3, ...
- What letter comes next in the sequence?
 E, T, A, O, I, N, S, H, ...
- In which row does Z go?
 A, E, F, H, I, K, L, M, N, T, V, W, X, Y
 B, C, D, G, J, O, P, Q, R, S, U
- What letter comes next in the sequence?
 W, L, C, N, I, T, ...

Symbols and signs

- The utility and power of symbols
- Choosing symbols, naming and pointing
- Symbols as "chunking" tools
- When to use symbols
 - 1. The importance of anonymity (e.g., the lambda calculus)
 - 2. Place holders (variables)
 - 3. Temporary and tentative symbols
- Signs, symbols, content and meaning

Intelligent patterning

- Creativity and Art
 - 1. Knowing when to pattern
 - Symbol attachment and creation; patterns/symbols as revealers and concealers
 - 3. Levels of patterning
- Multiple patterns and selection (x-1)(x-2)(x-3) - 6 $x^3 - 6x^2 + 11x - 12$ $(x-4)(x^2 - 2x + 3)$
- Adaptive pattern recognition
- Are the patterns really there?

Some history

- Physics
- Philosophy (theory of knowledge)
- Mathematics
 - 1. Matrix manipulation
 - 2. Topology
 - 3. Algebra
 - 4. Lie groups
 - 5. Manifolds and relativity theory
 - 6. Algebraic topology

We have the map $b_n: \Sigma^2 U(n) \to SU(n+1)$ given by

$$b_n(g,r,s) = [i(g), v_n(r,s)]$$

where i(g) is the inclusion, $[g,h] = ghg^{-1}h^{-1}$ and

 $v_n(r,s) =$

$$\begin{bmatrix} \alpha & 0 & 0 & \cdots & 0 & \beta(-\overline{\alpha})^{0} \\ \beta(-\overline{\alpha})^{0}\overline{\beta} & \alpha & 0 & \cdots & 0 & \beta(-\overline{\alpha})^{1} \\ \beta(-\overline{\alpha})^{1}\overline{\beta} & \beta(-\overline{\alpha})^{0}\overline{\beta} & \alpha & \cdots & 0 & \beta(-\overline{\alpha})^{2} \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ \beta(-\overline{\alpha})^{n-1}\overline{\beta} & \beta(-\overline{\alpha})^{n-2}\overline{\beta} & \cdots & \cdots & \alpha & \beta(-\overline{\alpha})^{n} \\ -(-\overline{\alpha})^{n}\overline{\beta} & -(-\overline{\alpha})^{n-1}\overline{\beta} & \cdots & \cdots & -(-\overline{\alpha})^{0}\overline{\beta} & -(-\overline{\alpha})^{n} \end{bmatrix}$$

where

$$\alpha = \alpha(r, s) = \cos(\pi r) + i \sin(\pi r) \cos(\pi s)$$
$$\beta = \beta(r, s) = i \sin(\pi r) \sin(\pi s)$$

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$ b_n: \Sigma^2U(n) \rightarrow SU(n+1) $ \newline
given by
[b_n(g, r, s) = [i(g), v_n(r, s) ]]
where i(g) is the inclusion,
\left[g, h\right] = ghg^{-1}h^{-1}\ \
and
v_n(r,s) = 
NΕ
\left[ \begin{array}{ccccc}
\alpha & 0 & 0 & \cdots & 0 & \beta (-\overline{\alpha})^0 \\
\beta (-\overline{\alpha})^0\overline{\beta} &
  \alpha & 0 & \cdots & 0 &
  \beta (-\overline{\alpha})^1 \\
\beta (-\overline{\alpha})^1\overline{\beta} &
  \beta (-\overline{\alpha})^0\overline{\beta} &
  \alpha & \cdots & 0 & \beta (-\overline{\alpha})^2 \\
\vdots & \vdots & \vdots & & \vdots \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
\vdots & \vdots & \vdots & & \vdots \\
\beta (-\overline{\alpha})^{n-1}\overline{\beta} &
  beta (-\verline{\alpha})^{n-2}\verline{\beta} &
  \cdots & \cdots & \alpha &
  \beta (-\overline{\alpha})^n \\
-(-\overline{\alpha})^n\overline{\beta} &
  -(-\operatorname{verline})^{n-1}\operatorname{verline} \&
  \cdots & \cdots & -(-\overline{\alpha})^0
  \overline{\beta} & -(-\overline{\alpha})^n \\
\end{array} \right]
\mathbf{1}
where
[ \  \  ] = \  \  ]
\cos(\pi r) + i \sin(\pi r)\cos(\pi s)
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What's wrong in computing today

- Not enough resolution on displays
- Not enough processing power and memory
- Not enough parallelism
- Software tools are "flat" and sequential rather than hierarchical

The intelligent mathematical assistant

- Adaptive symbolic input and output
- Strong basic skills (all of arithmetic through college calculus and elementary discrete structures)
- First order logic capabilities
- Adaptive "patterning" and "symboling"
- Elementary hypothesis generation and testing